## The First Transistor

Co-inventors of the first transistor at Bell Laboratories: Dr. William Shockley (seated); Dr. John Bardeen (left); Dr. Walter H. Brattain. (Courtesy of AT\&T
Archives.)
Dr. Shockley Born: London,
England, 1910 PhD Harvard, 1936
Dr. Bardeen Born: Madison, Wisconsin, 1908 PhD Princeton, 1936
Dr. Brattain Born: Amoy, China, 1902
PhD University of Minnesota, 1928
All shared the Nobel Prize in
1956 for this contribution.


## Construction

- 3-Layer Semiconductor device
- 2 p-layers and one n-layer or vise versa
- pnp or npn types
- Two pn junctions, each of them can be either forward or reverse biased
- This results in 4 possible modes of operation



## Bipolar junction Transistor_ (BJT):

BJT:
1.It's a semiconductor device that can amplify electı signals such as radio or television signals.

2. Its essential ingredient of every electronic circuits; from the simplest amplifier or oscillator to the most elaborate digital computer.
3. It's a three terminal device;

Base, Emitter, and Collector.

## There are two type of BJT:

$>$ npn type
$>$ pnp type


## Transistor structure:



Fall 2015-2016

## Transistor biasing:

$\checkmark$ In order to operate properly as an amplifier, it's necessary to correctly bias the two pn-junctions with external voltages.
$\checkmark$ Depending upon external bias voltage polarities used; the transistor works in one of four regions (modes). npn transistor modes of
$\checkmark$ For transistor to be used as an Active device (Amplifier); the emitter-base junction must be forward bias, while the collector-base junction must be reverse biased.

|  | operation |  |  |
| :---: | :---: | :---: | :---: |
| Junction/ Mode | BE | BC | Remarks |
| Saturation Mode | Forward | Forward | Equivalent to short circuit Ic=lc(sat) $\mathrm{Vce}=\mathrm{Vce}(\mathrm{sat})=\sim 0.2 \mathrm{~V}$ |
| Active Mode (Linear Region) | Forward | Reverse | Ic proportional to lb Vce defined by circuit |
| Cut-off Mode | Reverse | Reverse | Equivalent to open circuit $\mathrm{Ic}=\mathrm{Ib}=0$ <br> Vce defind by circuit |
| Inverse Mode | Reverse | Forward | Rarely used and will not be discussed in this course |

## In active region

$\checkmark$ The base region is thin and lightly doped
$\checkmark$ The emitter-base junction is forward biased, thus the depletion region at this junction is reduced.
$\checkmark$ The base-collector junction is reverse biased, thus the depletion region at this junction is increased.

$\checkmark$ The forward biased BE-junction causes the electrons in the n-type emitter to flow toward the base; this constitutes the emitter current $\boldsymbol{I}_{E}$.
$\checkmark$ As these electrons flow through the P-type base; they tend to recombine with holes in p -type base.
$\checkmark$ Since the base region is lightly doped; very few of the electrons injected into the base from the emitter recombine with holes to constitute base current $I_{B}$ and the remaining large number of electrons cross the base and move through the collector region to the positive terminal of the external DC source; this constitute collector current $I_{C}$
$\checkmark$ There is another component for $I_{C}$ due to the minority carrier; $I_{\text {Сво }}$

$I_{C}=\alpha I_{E}+I_{C B o}$
$I_{E}=I_{C}+I_{B}$
$I_{C}=\alpha\left(I_{C}+I_{B}\right)+I_{C B o}$
$\not I_{C}=\frac{\alpha}{1-\alpha} I_{B}+\frac{1}{1-\alpha} I_{C B O}$
Let Beta, $\beta=\frac{\alpha}{1-\alpha}$

$\boldsymbol{*}_{\boldsymbol{C}}=\beta \boldsymbol{I}_{\boldsymbol{B}}+(\beta+\mathbf{1}) \boldsymbol{I}_{\boldsymbol{C B}}$
$I_{C}=\beta I_{B}+I_{C E O}$
$\begin{array}{lll}\alpha=\frac{\alpha}{1-\alpha} & \begin{array}{l}\text { If } \alpha=0.99 \\ \text { If } \alpha=0.995 \\ \longrightarrow\end{array} & \beta=99 \\ \beta=199\end{array}$

## In active region:

$$
\begin{aligned}
& \boldsymbol{I}_{\boldsymbol{C}}=\boldsymbol{\alpha} \boldsymbol{I}_{\boldsymbol{E}}+\boldsymbol{I}_{\boldsymbol{C B o}} \\
& \boldsymbol{I}_{\boldsymbol{C}}=\beta \boldsymbol{I}_{\boldsymbol{B}}+(\beta+\mathbf{1}) \boldsymbol{I}_{\boldsymbol{C B o}} \\
& \boldsymbol{I}_{\boldsymbol{C}}=\beta \boldsymbol{I}_{\boldsymbol{B}}+\boldsymbol{I}_{\boldsymbol{C E} o} \\
& \boldsymbol{I}_{\boldsymbol{E}}=\boldsymbol{I}_{\boldsymbol{C}}+\boldsymbol{I}_{\boldsymbol{B}}
\end{aligned}
$$

$$
\beta=\frac{\alpha}{1-\alpha}
$$

Approximate relationships:
$I_{C} \cong \alpha I_{E} \cong I_{E}$
$I_{C} \cong \beta I_{B}$
$I_{E} \cong(\beta+1) I_{B}$

## Basic BJT Amplifiers Circuits

$\alpha \approx \frac{I_{C}}{I_{E}}$
BJT in Active Mode $\quad I_{\mathrm{E}}=I_{\mathrm{B}}+I_{\mathrm{C}}$ $\beta \approx \frac{I_{C}}{I_{B}} \quad$---common-emitter current gain
$\beta=\frac{\alpha}{1-\alpha}$

## BJT DC Analysis

- Make sure the BJT current equations
 and region of operation match

$$
\begin{aligned}
& V_{\mathrm{BE}}>0, \\
& V_{\mathrm{BC}}<0, \rightarrow V_{\mathrm{E}}<V_{\mathrm{B}}<V_{\mathrm{C}}
\end{aligned}
$$

- Utilize the relationships ( $\beta$ and $\alpha)$
between collector, base, and emitter
currents to solve for all currents $\left\{\begin{array}{l}I_{E}=I_{C}+I_{B}=(1+\beta) I_{B} \\ I_{C}=\beta I_{B} \\ I_{C}=\alpha I_{E}\end{array}\right.$


## Basic BJT Amplifiers Circuits

C-E Circuits I-V Characteristics
Base-emitter Characteristic(Input characteristic)


$i_{B(t)}=I_{B O}\left(e^{\frac{V_{B E}(t)}{\eta V_{T}}}-1\right)$
$i_{B(t)} \cong I_{B o}\left(e^{\frac{V_{B E}(t)}{\eta V_{T}}}\right)$

## Basic BJT Amplifiers Circuits

C-E Circuits I-V Characteristics
Collector characteristic (output characteristic)

$$
i_{C}=\left.f_{\left(V_{C E}\right)}\right|_{i_{B}=C}
$$





## Basic BJT Amplifiers Circuits

## C-E Circuits I-V Characteristics

Collector characteristic (output characteristic) $\quad i_{C}=\left.f_{\left(V_{C E}\right)}\right|_{i_{B}=C}$


## Basic BJT Amplifiers Circuits



Once the base current is high enough to produce saturation, further increases in base current have no effect on the collector current and the relationship $I_{C}=\beta I_{B}$ is no longer valid. When $V_{C E}$ reaches its saturation value, $V_{C E(\text { sat })}$, the base-collector junction becomes forward-biased.

## Basic BJT Amplifiers Circuits



## Basic BJT Amplifiers Circuits

## C-E Circuits I-V Characteristics

Collector characteristic


1. In the cutoff region :

$$
\boldsymbol{I}_{\boldsymbol{B}}=\boldsymbol{I}_{C}=\boldsymbol{I}_{E}=\mathbf{0}
$$

2. In the active region :

$$
\begin{aligned}
& I_{C}=\alpha I_{E} \\
& V_{B E}=0.8 v \quad, \quad \mathbf{S i} \quad, \quad n p n \\
& I_{C}=\beta I_{B} \\
& \boldsymbol{I}_{\boldsymbol{E}}=(\beta+\mathbf{1}) I_{\boldsymbol{B}} \\
& V_{B E}=0.7 v \quad, \quad \mathrm{Si} \quad, \quad \mathrm{npn} \\
& V_{B E}=-0.7 v \quad, \quad \text { Si } \quad, \quad \text { pnp } \\
& V_{C E}>V_{C E, s a t}=0.2 v, \quad \mathrm{Si}, \quad \mathrm{npn} \\
& V_{C E}<V_{C E, s a t}=-0.2 v, \quad \text { Si } \quad \text { pnp }
\end{aligned}
$$



## In General

1)In the active region:

$$
\begin{aligned}
& I_{B}=\frac{V_{B B}-V_{B E}}{R_{B}} \\
& I_{C}=\beta I_{B} \\
& V_{C E}=V_{C C}-R_{C} I_{C}
\end{aligned}
$$



$$
\text { As }: R_{B} \downarrow, I_{B} \uparrow, I_{C} \uparrow, V_{C E}
$$

2 ) In the saturation region:

$$
\begin{aligned}
& V_{C E}=V_{C E, s a t}=0.2 v \quad, \quad \mathrm{Si} \quad, \quad \mathrm{npn} \\
& I_{C}=I_{C, s a t}=\frac{V_{C C}-V_{C E, s a t}}{R_{C}}
\end{aligned}
$$

Assume that the transistor in the active region:
KVL: $\quad 5=200 k I_{B}+V_{B E}$

$$
\begin{aligned}
& I_{B}=\frac{5-0.7}{200 k}=0.0215 \mathrm{~mA} \\
& I_{C}=\beta I_{B}=100 * 0.0215=2.15 \mathrm{~mA} \\
& \text { KVL: } \quad 10=R_{C} I_{C}+V_{C E} \\
& V_{C E}=10-R_{C} I_{C} \\
& * V_{C E}=10-3 k * 2.15 m A=3.55 \mathrm{Volt}
\end{aligned}
$$

Since

$$
\begin{aligned}
& \quad V_{C E}>V_{C E, s a t} \ggg \text { The transistor is in the active region } \\
& >V_{C E Q}=3.55 \text { Volt } \\
& >I_{C Q}=2.15 \mathrm{~mA}
\end{aligned}
$$

Let define: $I_{B}(\min )=\frac{I_{C, \text { sat }}}{\beta}$


$I_{B}($ min $)=\frac{I_{C, \text { sat }}}{\beta}$
\& If $I_{B}>I_{B}(\min )$ the transistor is in the saturation region.
$\$$ If $I_{B}<I_{B}(\mathrm{~min})$ the transistor is in the Active region.

## Determine Mode of Operation of BJT?

- 1) Since $B E$ junction is forward biased $==>$ Q1 can be either in Active (Linear) or Saturation mode
- Assume it is in Active Mode

$$
\begin{aligned}
& 5=200 \mathrm{k} \Omega . \mathrm{I}_{\mathrm{B}}+\mathrm{V}_{\mathrm{BE}}+2 \mathrm{k} \Omega \cdot \mathrm{I}_{\mathrm{E}} \\
& \text { But, } \quad \mathrm{I}_{\mathrm{E}}=(1+\beta) \mathrm{I}_{\mathrm{B}} \\
& \text { Solve for } \mathrm{I}_{\mathrm{B}}=\frac{5-\mathrm{V}_{\mathrm{BE}}}{200 \mathrm{k} \Omega+(1+\beta) .2 \mathrm{k} \Omega} \\
& \mathrm{I}_{\mathrm{B}}=\frac{5-0.7}{200 \mathrm{k} \Omega+(1+100) .2 \mathrm{k} \Omega} \\
& =\frac{4.3 \mathrm{~V}}{402 \mathrm{k} \Omega}=10.7 \mu \mathrm{~A}
\end{aligned}
$$



$$
\begin{aligned}
& \mathrm{I}_{\mathrm{C}}=\beta \mathrm{I}_{\mathrm{B}} \\
& =(100) \cdot(10.7 \mu \mathrm{~A}) \\
& =1.07 \mathrm{~mA} \\
& \mathrm{I}_{\mathrm{E}}=(\beta+1) \mathrm{I}_{\mathrm{B}} \\
& =1.0807 \mathrm{~mA}
\end{aligned}
$$

Now we find $V_{C E}$ from output circuit
$10-\mathrm{I}_{\mathrm{C}} .3 \mathrm{k} \Omega-\mathrm{I}_{\mathrm{E}} .2 \mathrm{k} \Omega=\mathrm{V}_{\mathrm{CE}}$
$\Rightarrow \mathrm{V}_{\mathrm{CE}}=4.63 \mathrm{~V}>\mathrm{V}_{\mathrm{CE}(\text { sat })}$

$\therefore \mathrm{Q} 1$ is in active mode and the assumption is true we can also verify that the BC junction is reverse biassed which is required so that the BJT operates in active mode
$10-\mathrm{I}_{\mathrm{C}} .3 \mathrm{k} \Omega-\mathrm{I}_{\mathrm{E}} .2 \mathrm{k} \Omega=\mathrm{V}_{\mathrm{CE}}$
$\Rightarrow \mathrm{V}_{\mathrm{CE}}=\mathrm{V}_{\mathrm{CB}}-\mathrm{V}_{\mathrm{EB}}$
$\Rightarrow \mathrm{V}_{\mathrm{CB}}=\mathrm{V}_{\mathrm{CE}}-\mathrm{V}_{\mathrm{BE}}=4.63-0.7=3.93 \mathrm{~V}$
$\therefore \mathrm{V}_{\mathrm{BC}}=-\mathrm{V}_{\mathrm{CB}}=-3.33 \mathrm{~V}$
$B C$ junction is reverse biased


## OR Second method: Assume Saturation

- 1) Since $B E$ junction is forward biased ==> Q1 can be either in Active (Linear) or Saturation mode
- Assume it is in saturation mode:
$10-\mathrm{I}_{\mathrm{C}(\mathrm{san})} \cdot 3 \mathrm{k} \Omega-\mathrm{I}_{\mathrm{E}(\mathrm{san}} \cdot 2 \mathrm{k} \Omega=\mathrm{V}_{\mathrm{CE}(\mathrm{San})}$ assume $I_{E(s a t)}=I_{C(s a t)}$

$$
\begin{aligned}
& \therefore I_{C(\text { sat) })}=\frac{10-0.2}{5 \mathrm{k} \Omega}=1.96 \mathrm{~mA} \\
& I_{\mathrm{B} \text { (min) })}=\frac{I_{\mathrm{C}(\mathrm{sat})}}{\beta}=19.6 \mu \mathrm{~A}
\end{aligned}
$$



## BJT as switch:

## Example:

Find $V_{o}(t)$ for the input given below:



## Solution:

$*$ Let $V_{i}(t)=+12$ volt
Calculate $V_{t h} \& R_{t h}$

$R_{t h}=15 k / / 100 k=\frac{100 k * 15 k}{15 k+100 k}=13 k$
$V_{t h}=8.9$ volt Proof!!

Since the base emitter
junction is forward bias; the transistor could be either in the active or the saturation region

Assume that the transistor in the saturation region
$I_{C}=I_{C, s a t}=\frac{V_{C C}-V_{C E, s a t}}{R_{C}}=\frac{12-0.2}{2.2 k}=5.36 \mathrm{~mA}$
$I_{B}(\min )=\frac{I_{C, s a t}}{\beta}=\frac{5.36 \mathrm{~mA}}{30}=0.18 \mathrm{~mA}$

$$
I_{B}=\frac{V_{t h}-V_{B E}}{R_{T H}}=\frac{8.9-0.8}{13 k}=0.62 \mathrm{~mA}
$$

$\$$ Since $I_{B}>I_{B}(\min )$ the transistor is in the saturation region.

$$
\begin{aligned}
& \checkmark V_{o}=V_{C E, s a t}=0.2 \text { volt } \\
& \checkmark I_{C}=5.36 \mathrm{~mA}
\end{aligned}
$$

$$
\dot{\text { Let }} V_{i}(t)=0 \text { volt }
$$



Since $V_{\text {th }}=-1.56$ volt
Base emitter junction is revers biased the transistor in cutoff region

$$
\begin{aligned}
& \checkmark V_{o}=V_{C E}=12 \text { volt } \\
& \checkmark I_{C}=0 \mathrm{~mA}
\end{aligned}
$$

The circuit acts as inverter or not gate


